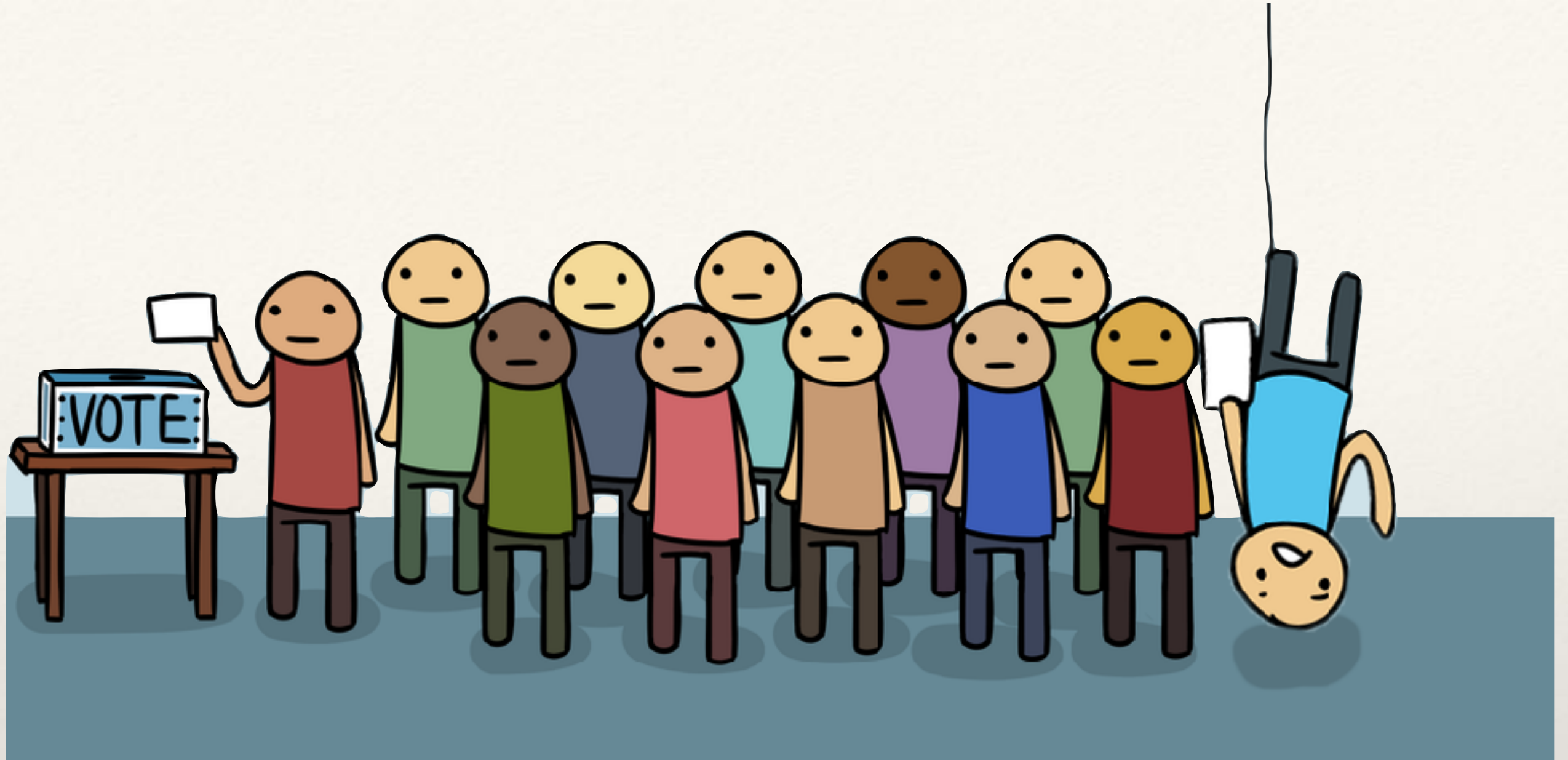




Condorcet's Principle and the Preference Reversal Paradox

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The Paradox

- ❖ Under many voting rules, it is sometimes better to report the *exact opposite* of your true preference ordering.

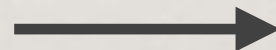
3	3	4	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>a</i>

d is Kemeny winner

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3	3	4	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>a</i>



3	3	3	1	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>

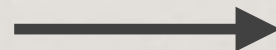
d is Kemeny winner

The Paradox

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3	3	4	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>a</i>

d is Kemeny winner



3	3	3	1	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>

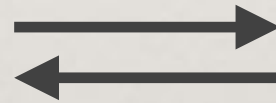
b is Kemeny winner

The Paradox

- ❖ Under many voting rules, it is sometimes better to report the *exact opposite* of your true preference ordering.

3	3	4	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>b</i>	<i>a</i>

d is Kemeny winner



3	3	3	1	2	3
<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>d</i>	<i>d</i>
<i>b</i>	<i>d</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>c</i>
<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>	<i>a</i>	<i>b</i>
<i>c</i>	<i>a</i>	<i>d</i>	<i>c</i>	<i>b</i>	<i>a</i>

b is Kemeny winner

Half-way monotonicity

- ❖ A voting rule satisfies **half-way monotonicity** if it avoids the paradox.
- ❖ $\Rightarrow$ always weakly better to report truth rather than reverse.
- ❖ Introduced by Sanver and Zwicker (IJGT 2009).

Good rules:

- ❖ Borda
- ❖ Plurality
- ❖ Scoring rules

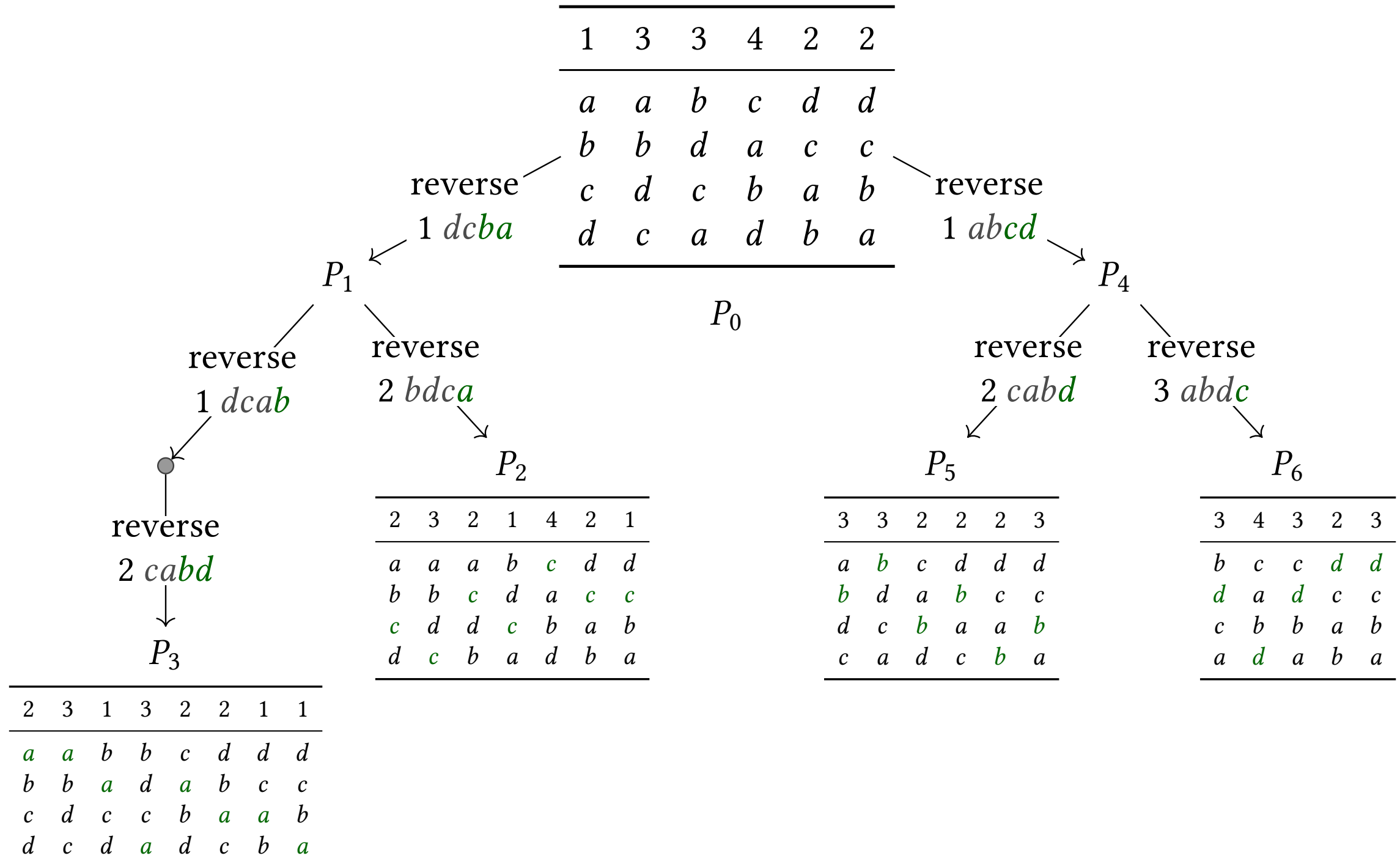
Bad rules:

- ❖ STV / Baldwin / Coombs
- ❖ Kemeny / maximin / Copeland / Schulze / Ranked Pairs
- ❖ Condorcet extensions
i.e. rules that select the Condorcet winner if it exists

Impossibility Theorem

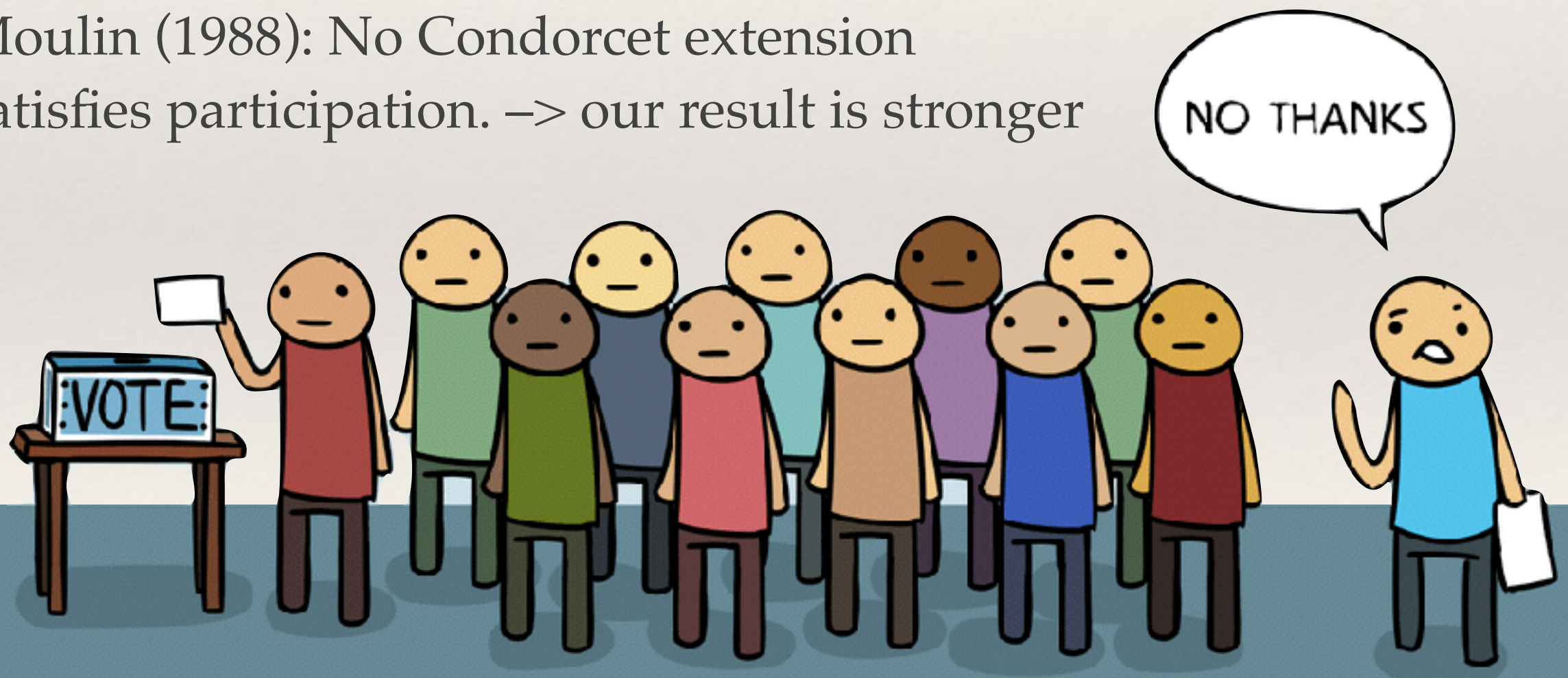
- ❖ Sanver and Zwicker (2009): **No Condorcet extension satisfies half-way monotonicity if there are $m \geq 4$ alternatives and sufficiently many voters.**
- ❖ Proof needs $n = 702 + \Omega(m!)$ voters, and n even.
- ❖ Unfortunately, their proof contains an arithmetical mistake, non-trivial to fix.
- ❖ Is the paradox a problem in small electorates?
- ❖ **We show the result holds for $n = 15$.**

Proof.

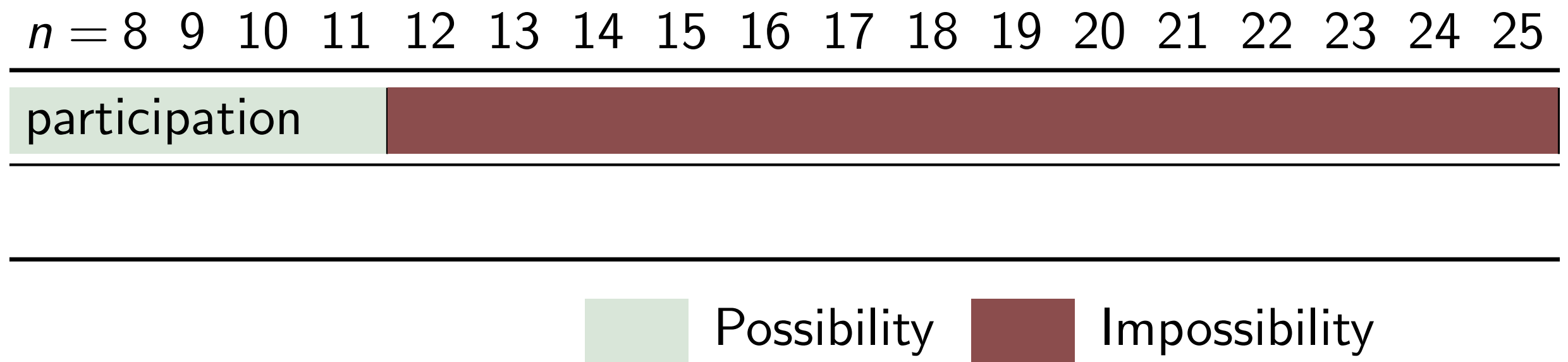


Comparison to Participation

- ❖ Voting rule satisfies **participation** if it is always weakly better to participate than to abstain ($\rightarrow$ avoid **no-show paradox**).
- ❖ participation $\Rightarrow$ half-way monotonicity
- ❖ Moulin (1988): No Condorcet extension satisfies participation. $\rightarrow$ our result is stronger

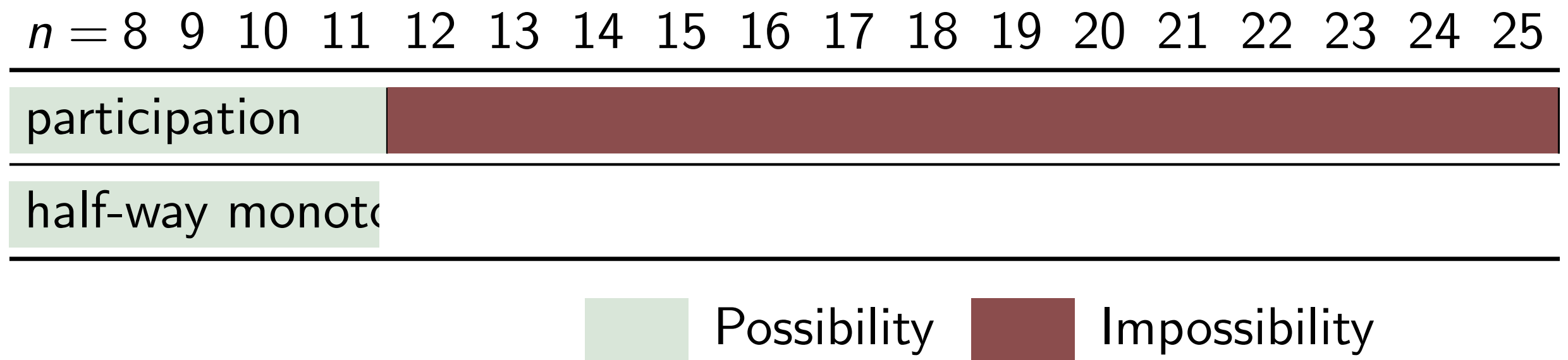


Number of Voters Required



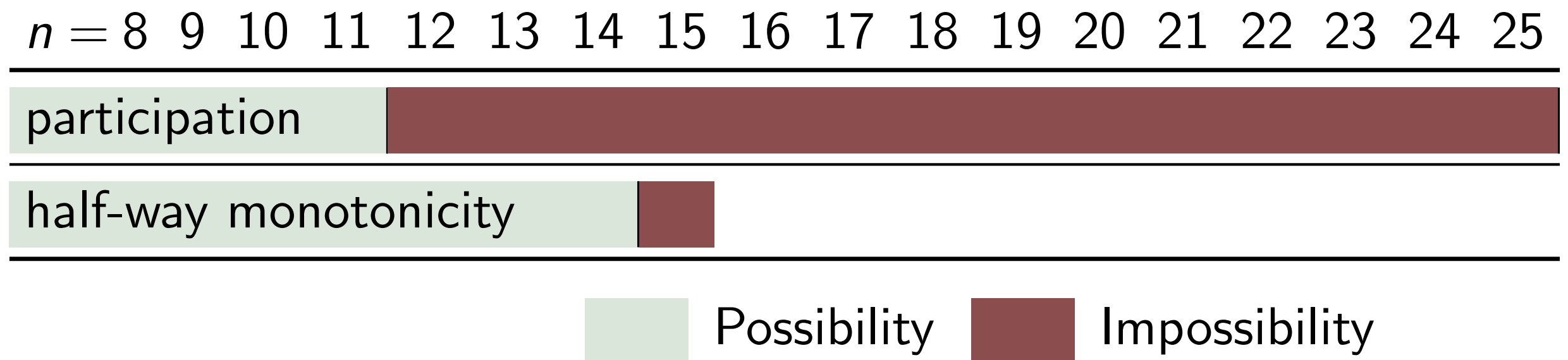
Brandt, Geist, P. (AAMAS 2016): For $m = 4$, participation is compatible with Condorcet consistency for $n = 11$, but incompatible for $n \geq 12$.

Number of Voters Required



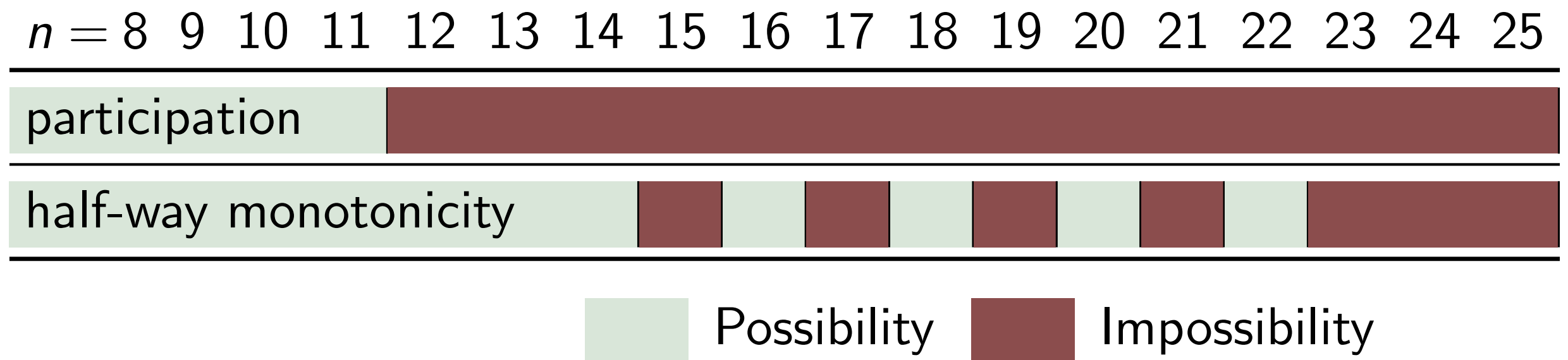
Brandt, Geist, P. (AAMAS 2016): For $m = 4$, participation is compatible with Condorcet consistency for $n = 11$, but incompatible for $n \geq 12$.

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Method: Impossibility Theorems via SAT Solving

- ❖ For fixed n and m , write a formula of propositional logic whose models correspond to good voting rules.
- ❖ Give to state-of-the-art SAT solver (e.g., lingeling, glucose)
- ❖ SAT $\Rightarrow$ good rule given by a look-up table
- ❖ UNSAT $\Rightarrow$ impossibility result
- ❖ Induction steps on n and m



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- ❖ More info in book chapter: Geist and P., Computer-aided Methods for Social Choice Theory. In Ulle Endriss (ed.), *Trends in Computational Social Choice* (forthcoming).

Encoding

- *functionality* of f , i.e., that $f(P) = a$ for exactly one alternative, which means that there is *at least* one and *at most* one such alternative:

$$\varphi_{\text{functionality}} \equiv \bigwedge_{P \in A!^N} \left(\left(\bigvee_{a \in A} x_{P,a} \right) \wedge \bigwedge_{a \neq b \in A} (\neg x_{P,a} \vee \neg x_{P,b}) \right)$$

- *Condorcet-consistency*: for $a \in A$, let $C_a \subseteq A!^N$ be the set of profiles in which a is the Condorcet winner.

$$\varphi_{\text{Condorcet}} \equiv \bigwedge_{a \in A} \bigwedge_{P \in C_a} x_{P,a}$$

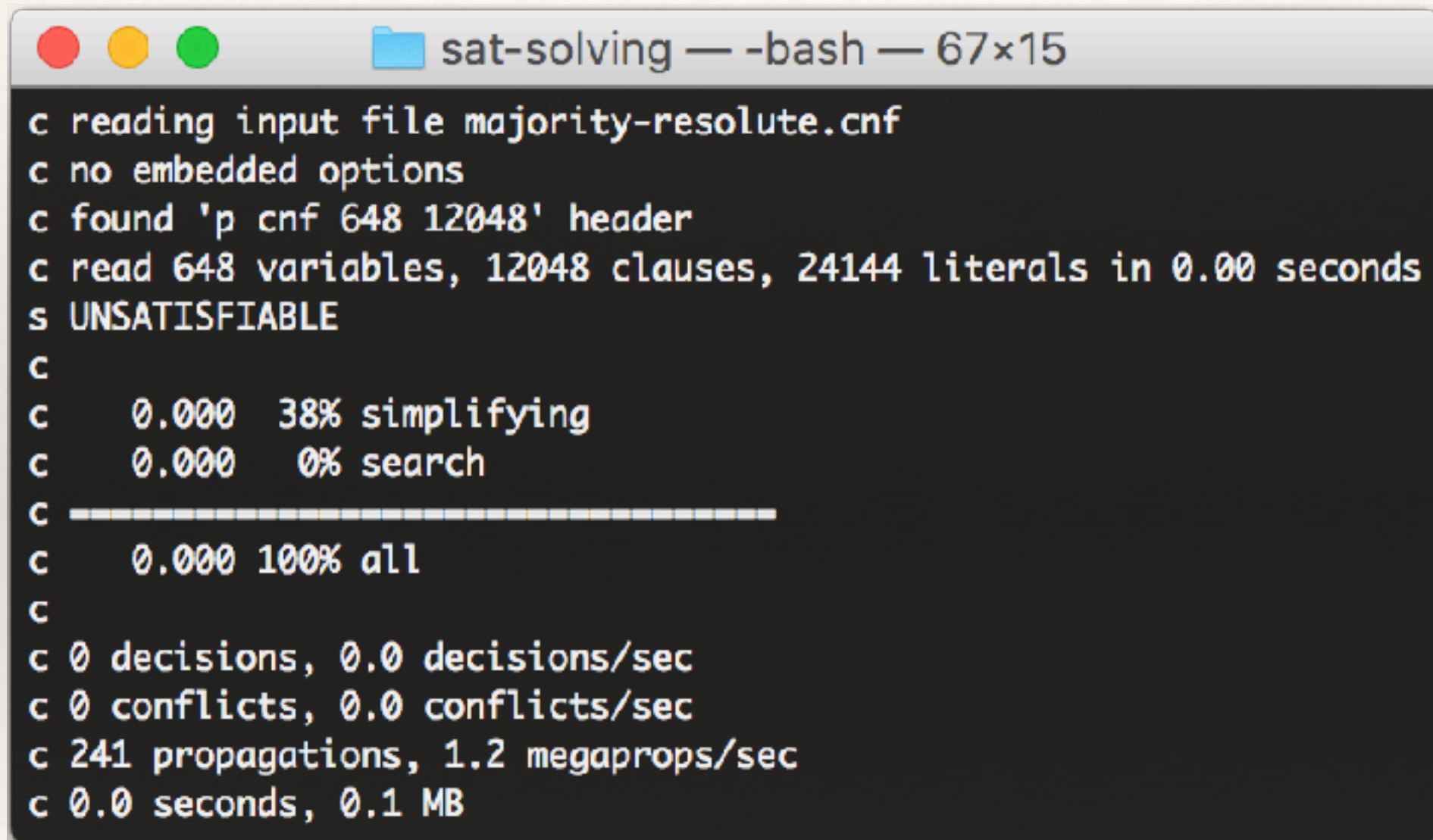
- *half-way monotonicity*: if $a, b \in A$ are such that $a \succ_i b$ for voter i in profile $P \in A!^N$, and $f(P) = b$, then $f(P_{-i}, \succ_i^{\text{rev}}) \neq a$.

$$\varphi_{\text{half-way monotonicity}} \equiv \bigwedge_{i \in N} \bigwedge_{P \in A!^N} \bigwedge_{\substack{a, b \in A \\ a \succ_i b}} (\neg v_{P,b} \vee \neg v_{(P_{-i}, \succ_i^{\text{rev}}), a}).$$

Satisfiability $\rightarrow$ Lookup-Table

A,#1,(1,1,1,1,1)	A,#2,(2,2,0,2,0,0)	A,#2,(2,2,2,-2,-2,0)	B,#2,(-2,2,0,2,2,0)	B,#2,(-2,2,-2,2,2,-2)	C,#2,(-2,-2,-2,-2,0,0)	B,#3,(-1,1,1,3,3,-1)
A,#1,(1,1,1,1,1,-1)	A,#2,(2,2,0,0,0,0)	A,#2,(0,2,2,0,0,2)	B,#2,(-2,0,0,2,2,0)	B,#2,(-2,0,-2,2,2,-2)	C,#2,(2,-2,-2,-2,-2,2)	B,#3,(-1,3,1,3,3,-3)
A,#1,(1,1,1,-1,1,1)	B,#2,(0,2,0,2,0,0)	A,#2,(0,2,2,0,0,0)	B,#2,(-2,0,2,0,2,2)	B,#2,(-2,0,-2,0,2,0)	C,#2,(0,-2,-2,-2,-2,2)	B,#3,(-1,1,1,3,3,-3)
A,#1,(1,1,1,-1,-1,1)	B,#2,(0,0,0,2,0,0)	C,#2,(0,0,2,0,0,2)	B,#2,(-2,0,0,0,2,2)	D,#2,(-2,0,-2,0,0,0)	D,#2,(2,0,-2,0,-2,0)	A,#3,(1,1,3,1,3,-1)
A,#1,(1,1,1,1,-1,-1)	A,#2,(2,0,0,0,0,0)	A,#2,(2,0,2,-2,-2,2)	C,#2,(-2,0,0,0,0,2)	D,#2,(0,2,-2,2,0,-2)	D,#2,(2,0,-2,-2,-2,0)	A,#3,(1,1,3,1,1,-1)
A,#1,(1,1,1,-1,-1,-1)	D,#2,(0,0,0,0,0,0)	C,#2,(0,0,2,-2,0,2)	B,#2,(-2,2,0,2,0,0)	D,#2,(0,2,-2,0,0,-2)	D,#2,(0,0,-2,0,-2,0)	B,#3,(-1,1,3,1,3,-1)
B,#1,(-1,1,1,1,1,1)	A,#2,(2,2,2,2,2,-2)	C,#2,(2,0,0,-2,-2,2)	B,#2,(-2,0,0,2,0,0)	B,#2,(-2,2,-2,2,0,-2)	D,#2,(0,-2,-2,0,-2,0)	B,#3,(-1,1,1,1,3,-1)
B,#1,(-1,1,1,1,1,-1)	A,#2,(2,2,2,0,2,0)	C,#2,(0,0,0,-2,-2,2)	B,#2,(-2,0,0,0,0,0)	B,#2,(-2,0,-2,2,0,-2)	C,#2,(2,-2,-2,-2,-2,0)	A,#3,(1,3,1,3,1,-3)
B,#1,(-1,-1,1,1,1,1)	A,#2,(2,2,2,2,0,-2)	A,#2,(2,2,0,0,-2,0)	B,#2,(-2,2,2,2,2,-2)	D,#2,(0,0,-2,0,0,-2)	C,#2,(0,-2,-2,-2,-2,0)	A,#3,(1,3,1,1,1,-3)
B,#1,(-1,-1,-1,1,1,1)	A,#2,(2,2,2,0,0,-2)	A,#2,(2,2,0,-2,-2,0)	B,#2,(-2,0,2,2,2,0)	D,#2,(-2,0,-2,0,0,-2)	C,#2,(-2,-2,-2,-2,-2,2)	B,#3,(-1,3,1,3,1,-3)
B,#1,(-1,-1,-1,1,1,-1)	A,#2,(0,2,2,2,2,-2)	D,#2,(0,2,0,0,-2,0)	B,#2,(-2,2,0,2,2,-2)	B,#2,(-2,-2,-2,2,2,-2)	D,#2,(0,0,-2,-2,-2,0)	B,#3,(-1,1,1,3,1,-3)
B,#1,(-1,-1,-1,1,1,-1)	B,#2,(0,0,2,2,2,0)	D,#2,(0,0,0,0,-2,0)	B,#2,(-2,0,0,2,2,-2)	C,#2,(0,-2,0,0,2,0)	D,#2,(-2,0,-2,0,-2,0)	A,#3,(1,1,1,1,1,-3)
C,#1,(1,-1,1,-1,1,1)	B,#2,(0,2,0,2,2,-2)	A,#2,(2,0,0,-2,-2,0)	B,#2,(-2,0,2,0,2,0)	B,#2,(-2,-2,0,0,2,0)	D,#2,(-2,-2,-2,0,-2,0)	B,#3,(-1,1,1,1,1,-3)
C,#1,(1,-1,1,-1,-1,1)	B,#2,(0,0,0,2,2,-2)	D,#2,(0,0,0,-2,-2,0)	B,#2,(-2,0,0,0,2,0)	B,#2,(-2,-2,-2,0,2,0)	C,#2,(-2,-2,-2,-2,-2,0)	A,#3,(1,-1,3,1,1,3)
C,#1,(-1,-1,1,-1,1,1)	A,#2,(2,0,2,0,2,0)	A,#2,(2,2,2,2,-2,-2)	B,#2,(-2,2,0,2,0,-2)	D,#2,(0,0,-2,2,0,-2)	D,#2,(2,2,-2,2,-2,-2)	A,#3,(1,-1,3,1,1,1)
C,#1,(-1,-1,-1,-1,1,1)	A,#2,(2,0,2,0,0,0)	A,#2,(2,2,2,0,-2,-2)	B,#2,(-2,0,0,2,0,-2)	B,#2,(-2,-2,-2,2,0,-2)	D,#2,(2,2,-2,0,-2,-2)	C,#3,(1,-1,3,-1,1,3)
C,#1,(1,-1,-1,-1,-1,1)	A,#2,(0,0,2,0,2,0)	A,#2,(0,2,2,2,0,0)	D,#2,(-2,0,0,0,0,-2)	D,#2,(0,-2,-2,0,0,-2)	D,#2,(0,2,-2,2,-2,-2)	C,#3,(1,-1,3,-1,-1,3)
C,#1,(-1,-1,-1,-1,-1,1)	B,#2,(0,0,0,0,2,0)	A,#2,(0,2,2,2,0,-2)	B,#2,(-2,-2,2,2,2,2)	D,#2,(-2,-2,-2,0,0,-2)	D,#2,(0,0,-2,2,-2,-2)	C,#3,(1,-1,3,1,-1,1)
D,#1,(1,1,-1,1,-1,-1)	A,#2,(2,2,0,2,0,-2)	B,#2,(0,0,2,2,0,0)	B,#2,(-2,-2,0,2,2,2)	C,#2,(2,-2,2,-2,2,2)	D,#2,(2,0,-2,0,-2,-2)	C,#3,(1,-1,3,-1,-1,1)
D,#1,(1,1,1,-1,-1,-1)	A,#2,(2,2,0,0,0,-2)	A,#2,(2,0,2,0,-2,0)	B,#2,(-2,-2,0,2,2,0)	C,#2,(2,-2,2,-2,0,2)	D,#2,(0,0,-2,0,-2,-2)	B,#3,(-1,-1,3,1,1,3)
D,#1,(-1,1,1,-1,-1,-1)	A,#2,(0,2,0,2,0,-2)	A,#2,(0,0,2,0,0,0)	C,#2,(0,-2,2,0,2,2)	C,#2,(0,-2,2,-2,2,2)	D,#2,(2,2,-2,-2,-2,-2)	B,#3,(-1,-1,3,1,1,1)
D,#1,(-1,-1,1,1,-1,-1)	D,#2,(0,0,0,2,0,-2)	D,#2,(2,0,0,0,-2,0)	C,#2,(0,-2,2,0,0,2)	C,#2,(0,-2,0,-2,2,2)	D,#2,(0,2,-2,0,-2,-2)	B,#3,(-1,-3,3,1,1,3)
D,#1,(1,-1,-1,-1,-1,-1)	D,#2,(2,0,0,0,0,-2)	A,#2,(2,2,0,2,-2,-2)	B,#2,(-2,-2,2,0,2,2)	C,#2,(2,-2,0,-2,0,2)	D,#2,(2,0,-2,-2,-2,-2)	B,#3,(-1,-3,1,1,1,3)
D,#1,(-1,-1,-1,-1,-1,-1)	D,#2,(0,0,0,0,0,-2)	A,#2,(2,2,0,0,-2,-2)	C,#2,(0,-2,0,0,2,2)	C,#2,(0,-2,0,-2,0,2)	D,#2,(0,0,-2,-2,-2,-2)	B,#3,(-1,-3,1,1,1,1)
A,#2,(2,2,2,2,2,2)	A,#2,(2,2,2,-2,2,2)	D,#2,(0,2,0,2,-2,-2)	C,#2,(2,2,0,0,0,2)	C,#2,(2,-2,0,-2,0,0)	D,#2,(-2,2,-2,2,-2,-2)	C,#3,(1,-3,3,-1,1,3)
A,#2,(2,2,2,2,2,0)	A,#2,(2,2,2,-2,0,2)	D,#2,(0,0,0,2,-2,-2)	C,#2,(-2,-2,0,0,0,2)	C,#2,(0,-2,0,-2,0,0)	D,#2,(-2,0,-2,2,-2,-2)	C,#3,(1,-3,3,-1,-1,3)
A,#2,(2,2,2,0,2,2)	A,#2,(2,2,2,-2,0,0)	D,#2,(2,0,0,0,-2,-2)	B,#2,(-2,-2,0,2,0,0)	C,#2,(2,-2,2,-2,-2,2)	D,#2,(-2,0,-2,0,-2,-2)	C,#3,(-1,-3,3,-1,1,3)
A,#2,(2,2,2,0,0,2)	A,#2,(0,2,2,0,2,2)	D,#2,(0,0,0,0,-2,-2)	C,#2,(0,-2,0,0,0,0)	C,#2,(0,-2,2,-2,0,2)	D,#2,(-2,-2,-2,2,-2,-2)	C,#3,(-1,-3,1,-1,1,3)
A,#2,(2,2,2,2,0,0)	A,#2,(0,2,2,0,2,0)	A,#2,(2,2,2,-2,-2,-2)	B,#2,(-2,-2,0,0,0,0)	C,#2,(2,-2,0,-2,-2,2)	D,#2,(0,-2,-2,0,-2,-2)	C,#3,(1,-3,1,-1,-1,3)
A,#2,(2,2,2,0,0,0)	B,#2,(0,2,0,0,2,0)	A,#2,(0,2,2,0,0,-2)	B,#2,(-2,-2,-2,2,2,2)	C,#2,(0,-2,0,-2,-2,2)	D,#2,(-2,-2,-2,0,-2,-2)	C,#3,(-1,-3,1,-1,-1,3)
A,#2,(0,2,2,2,2,2)	A,#2,(2,0,2,-2,2,2)	D,#2,(0,2,0,0,0,-2)	B,#2,(-2,0,-2,2,2,0)	D,#2,(0,-2,0,0,-2,0)	D,#2,(2,-2,-2,-2,-2,-2)	D,#3,(1,-1,1,1,-1,1)
A,#2,(0,2,2,2,2,0)	A,#2,(2,0,2,-2,0,2)	A,#2,(2,0,2,-2,0,0)	B,#2,(-2,-2,-2,2,2,0)	C,#2,(2,-2,0,-2,-2,0)	D,#2,(0,-2,-2,-2,-2,-2)	D,#3,(-1,-1,1,1,-1,1)
B,#2,(0,0,2,2,2,2)	C,#2,(0,0,2,-2,2,2)	A,#2,(2,0,2,-2,-2,0)	C,#2,(0,-2,0,0,2,2)	C,#2,(0,-2,0,-2,-2,0)	D,#2,(-2,-2,-2,-2,-2,-2)	D,#3,(-1,-3,1,1,-1,1)
B,#2,(0,0,0,2,2,2)	C,#2,(0,0,0,-2,2,2)	C,#2,(0,0,2,-2,0,0)	B,#2,(-2,-2,-2,0,2,2)	C,#2,(-2,-2,2,-2,2,2)	A,#3,(1,3,3,3,3,-1)	C,#3,(1,-3,1,-1,-1,1)
B,#2,(0,2,0,2,2,0)	C,#2,(2,0,0,-2,0,2)	A,#2,(2,2,0,-2,-2,-2)	C,#2,(0,-2,-2,0,0,2)	C,#2,(-2,-2,0,-2,2,2)	A,#3,(1,3,3,1,3,-1)	C,#3,(-1,-3,1,-1,-1,1)
B,#2,(0,0,0,2,2,0)	C,#2,(0,0,0,-2,0,2)	D,#2,(0,2,0,0,-2,-2)	C,#2,(-2,-2,-2,0,0,2)	C,#2,(-2,-2,0,-2,0,2)	A,#3,(1,3,3,1,1,-1)	C,#3,(1,-1,3,-1,3,3)
A,#2,(2,0,2,0,2,2)	A,#2,(2,2,0,-2,0,0)	D,#2,(2,0,0,-2,-2,-2)	D,#2,(0,0,-2,2,0,0)	C,#2,(-2,-2,0,-2,0,0)	A,#3,(1,3,3,1,1,-1)	C,#3,(1,-1,3,-1,3,1)
A,#2,(2,0,2,0,0,2)	A,#2,(0,2,0,0,0,0)	D,#2,(0,0,0,-2,-2,-2)	D,#2,(0,0,-2,0,0,0)	C,#2,(-2,-2,-2,-2,2,2)	A,#3,(1,3,3,3,1,-3)	C,#3,(1,-1,3,-3,3,3)
C,#2,(0,0,2,0,2,2)	C,#2,(2,0,0,-2,0,0)	B,#2,(-2,2,2,2,2,2)	B,#2,(-2,0,-2,2,0,0)	C,#2,(0,-2,-2,-2,0,2)	A,#3,(1,3,3,1,1,-3)	C,#3,(1,-1,3,-3,1,3)
C,#2,(0,0,0,0,2,2)	C,#2,(0,0,0,-2,0,0)	B,#2,(-2,2,2,2,2,0)	B,#2,(-2,-2,-2,2,0,0)	C,#2,(-2,-2,-2,-2,0,2)	B,#3,(-1,3,3,3,3,-1)	C,#3,(1,-1,3,-1,1,1)
C,#2,(2,0,0,0,0,2)	A,#2,(2,2,2,-2,-2,2)	B,#2,(-2,0,2,2,2,2)	D,#2,(0,-2,-2,0,0,0)	D,#2,(0,0,-2,-2,0,0)	B,#3,(-1,3,3,3,3,-3)	C,#3,(1,-1,3,-3,1,1)
C,#2,(0,0,0,0,0,2)	A,#2,(2,2,2,0,-2,0)	B,#2,(-2,0,0,2,2,2)	B,#2,(-2,-2,-2,0,0,0)	C,#2,(0,-2,-2,-2,0,0)	B,#3,(-1,1,3,3,3,-1)	C,#3,(-1,-1,3,-1,3,3)

Unsatisfiability – Proof?

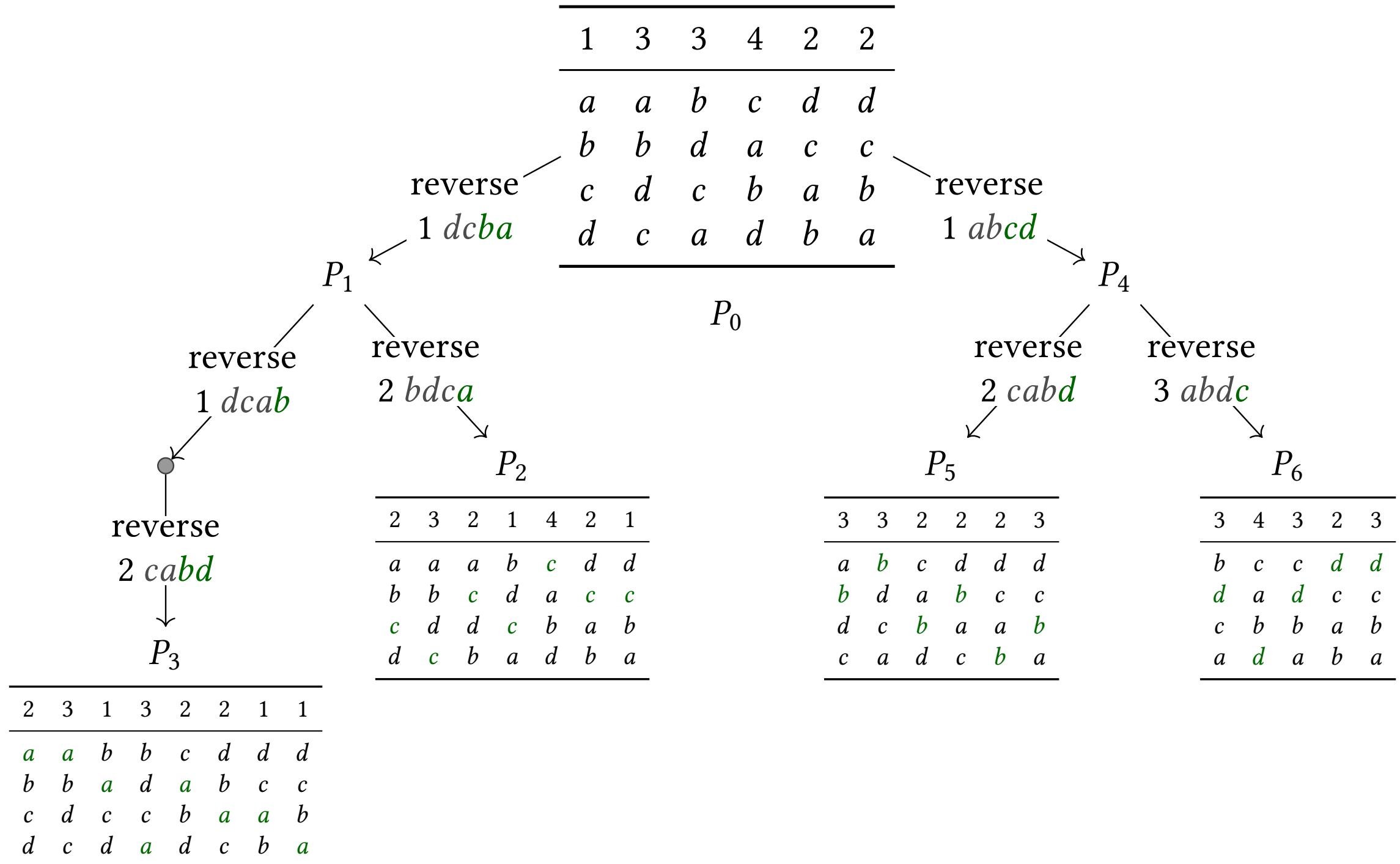


```
sat-solving — -bash — 67x15
c reading input file majority-resolute.cnf
c no embedded options
c found 'p cnf 648 12048' header
c read 648 variables, 12048 clauses, 24144 literals in 0.00 seconds
s UNSATISFIABLE
c
c 0.000 38% simplifying
c 0.000 0% search
c -----
c 0.000 100% all
c
c 0 decisions, 0.0 decisions/sec
c 0 conflicts, 0.0 conflicts/sec
c 241 propagations, 1.2 megaprops/sec
c 0.0 seconds, 0.1 MB
```

Unsatisfiability – Proof?

- ❖ Use Minimal Unsatisfiable Sets (MUS)
- ❖ Subselection of the clauses, already unsatisfiable
- ❖ Removing any clause yields satisfiability
- ❖ $\Rightarrow$ every clause in MUS is “necessary proof step”
- ❖ Fast tools to find an MUS (e.g. MUSer2, MARCO)
- ❖ If small, can obtain a **human-readable proof**

Proof.



Other Examples of the Method

- ❖ No Pareto-optimal **tournament solution** is strategyproof (Brandt and Geist, JAIR 2016) nor satisfies participation (Brandl et al, IJCAI 2015)
- ❖ No **probabilistic voting rule** is efficient and strategyproof (Brandl, Brandt, Eberl, Geist, JACM 2017)
- ❖ Impossibilities for **set extensions** (Geist and Endriss, JAIR 2011).
- ❖ Proofs of **Arrow's** and **Gibbard–Satterthwaite** Theorem (Tang and Lin, AIJ 2009)
- ❖ No strategyproof and proportional **multiwinner rules** (P., working paper)
- ❖ *many other possible applications..*

Results in the Paper

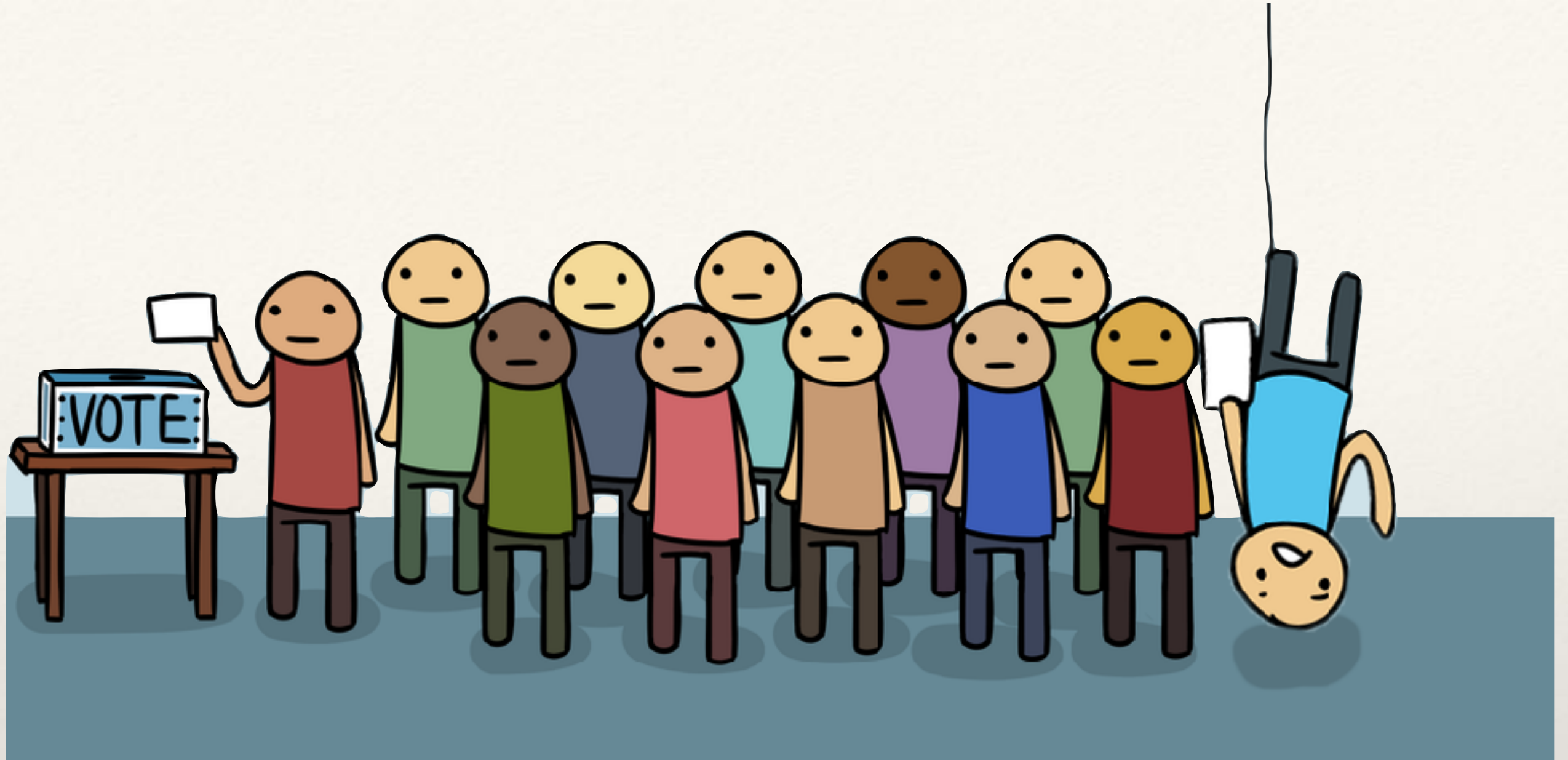
- ❖ Incompatibility for $n = 15$ and 24
- ❖ Induction steps for $m + 1$ and $n + 2$
- ❖ Set-valued voting rules (optimists and pessimists)
- ❖ Strong preference reversal paradox (which most Condorcet extensions except maximin exhibit)
- ❖ A version of the Gibbard–Satterthwaite Theorem

Disjunctive Gibbard–Satterthwaite

- ❖ **Every anonymous, unanimous voting rule is either *needlessly or egregiously* manipulable.** ($n \geq 15$ odd, $m \geq 4$)
- ❖ Idea for this type of result appears in Zwicker (2016, Handbook of COMSOC)
- ❖ Proof:
 - ❖ If the voting rule is a Condorcet extension, then it is manipulable by preference reversal.
 - ❖ If the voting rule is *not* a Condorcet extension, then by the Campbell–Kelly Theorem (2003, Econ Theory), the rule is manipulable between two profiles with a Condorcet winner, since the Condorcet rule is the only (non-trivial) strategyproof rule on Condorcet profiles.

Future Work

- ❖ Find other versions of G–S with restricted manipulations
 - ❖ e.g., known that G–S holds even if manipulators only perform a single swap (Caragiannis et al, EC 2012; Sato, JET 2013)
- ❖ Analogue of G–S result for Duggan–Schwartz
- ❖ Find concise description of positive examples
- ❖ What happens for $m \geq 5$?



Condorcet's Principle and the Preference Reversal Paradox

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